## Ashwaní Gupta

## Class - $\underline{\mathrm{X}}$

## Mathematics

## GENERAL INSTRUCTIONS:

1. All questions are compulsory.
2. The question paper consists of thirty four questions divided into four sections $A, B, C \mathcal{E} D$. Section $A$ comprises of ten questions of 01 marks each, Section B comprises of eight questions of 02 marks each, Section C comprises often questions of 03 marks each and section D comprises of six questions of 04 marks each.
3. All questions in section A are multiple choice questions where you are to select one correct option out of given four.
4. There is no overall choice. However internal choice has been provided in one question of 02 marks each, three questions of 03 marks each and two questions of 04 mark each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculators is not permitted.

## Section - 'A'

1. If $x=\frac{2}{3}$ is a solution of the equation $k x^{2}-x-2=0$, then the value of $k$ is:
(a) $k=-6$
(b) $k=6$
(c) $k=3$
(d) $k=2$
2. If $4 k+8,2 x^{2}+3 k+6,3 k^{2}+4 k+4$ are the three successive terms of an A.P., then the value opf $k$ is:
(a) 0 or 1
(b) 0 or 2
(c) 1 or 2
(d) 0 or -2
3. Two consecutive circles are of radii 5 cm and 3 cm . The length of the chord of the larger circle touches the smaller circle is:
(a) 4 cm
(b) 8 cm
(c) 7 cm
(d) 9 cm
4. A point ' $A$ ' is 13 cm from the centre of the circle. The length of the tangent drawn from ' $A$ ' to the circle is 12 cm . The radius of the circle is:
(a) $\overline{313} \mathrm{~cm}$
(b) 5 cm
(c) 8 cm
(d) 10 cm
5. If all the sides of a parallelogram touches the circle, than the parallelogram is:
(a) square
(b) rhombus
(c) rectangle
(d) kite
6. If TP \& TQ are two tangents to a circle with centre O so that $\angle P O Q=80^{\circ}$, then $\angle P T Q$ is equal to:
(a) $60^{\circ}$
(b) $100^{\circ}$
(c) $70^{\circ}$
(d) $120^{\circ}$
7. Three solid spheres of radii $3 \mathrm{~cm}, 4 \mathrm{~cm}$ and 5 cm respectively are melted \& converted into a single solid sphere. The radii of the sphere is:
(a) 12 cm
(b) 6 cm
(c) 8 cm
(d) 10 cm

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8. The area of sector of a circle whose radius is $14 \mathrm{~cm} \&$ the angle of sector is $45^{\circ}$, is:
(a) $66 \mathrm{~cm}^{2}$
(b) $77.5 \mathrm{~cm}^{2}$
(c) $77 \mathrm{~cm}^{2}$
(d) $88 \mathrm{~cm}^{2}$
9. If the altitude of the sun is $60^{\circ}$, then the height of the vertical tower that will cast a shadow of length 30 m is:
(a) $30 \overline{3} \mathrm{~m}$
(b) 15 m
(c) $\frac{30}{3} \mathrm{~cm}$
(d) $15 \overline{2} \mathrm{~m}$
10. Out of 15 boys and 10 girls of a class, one student is to be selected as monitor of the class. The probability of selecting a girl is:
(a) $\frac{2}{3}$
(b) $\frac{3}{2}$
(c) $\frac{2}{5}$
(d) $-\frac{2}{5}$

## Section - 'B'

11. Solve for $x$ : $36 x^{2}-12 a x+a^{2}-b^{2}=0$
12. Find the sum of all three digit numbers which are multiple of
13. The length of a tangent drawn from a point $Q$ outside the circle is 16 cm . The radius of the circle is 12 cm . Find the distance between $Q$ \& the centre of the circle.
14. Find the area of a ring shaped region enclosed between two concentric circles of radii $20 \mathrm{~cm} \& 15 \mathrm{~cm}$.
15. A cubical block of side 7 cm is surmounted by a hemisphere. What is the greatest diameter the sphere can have? Find the surface area of the solid.
16. Find the co-ordinates of a point which divides the join of $-1,7 \& 4,-3$ in the ratio $2: 3$.
17. Find the value of ' $k$ ' for which the following points are collinear: $7,-2,5,1,3, k$.
18. A pair of dice is thrown once, find the probability of getting a total of 11 .

## OR

Find the probability of two friends having (i) different birthdays (ii) the same birthdays (assuming that none of them is born in a leap year).

## Section - 'C'

19. Find the roots of the following equation, if they exist:
$\frac{x+2}{x+1}+\frac{x+4}{x+3}=\frac{x+3}{x+2}+\frac{x+5}{x+4}, \quad x \neq-1,3,-2,-4$

## OR

The difference of squares of two natural numbers is 45 . The square of the smaller number is four times the larger number. Find the numbers.
20. In an A.P. the sum of its first $n$ terms is $n^{2}+2 n$. Find the $16^{\text {th }}$ term.
21. In the given figure, two circles touch each other externally at C . Prove that the common tangent at C bisects the other two common tangents.


OR
$P Q \& P R$ are the tangents of the circle with centre $O$. $P S$ passes through $O$. If $P Q=12 \mathrm{~cm}, O Q=5 \mathrm{~cm}$. Find $P S$.

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22. Construct a $\triangle A B C$ in which $A B=4.5 \mathrm{~cm}, B C=5 \mathrm{~cm}$ \& angle $B=60^{\circ}$. Draw a triangle similar to $\triangle A B C$ whose sides are $\frac{3}{2}$ of the corresponding sides of $\triangle \mathrm{ABC}$.
23. Three horses are tethered with a 7 m long rope at the three corners of a triangular field having sides $20 \mathrm{~m}, 34 \mathrm{~m} \& 42 \mathrm{~m}$. Find the area
24. A container made up of a metal sheet is in the form of a frustum of a cone of height 16 cm with radii of its lower \& upper end as 8 cm and 20 cm respectively. Find the cost of the milk which can completely fill the container at the rate of Rs20 per litre.

## OR

A toy is in the form of a cone mounted on a hemisphere of radius 3.5 cm . If the total height of the toy is 15.5 cm , find its total surface area of the toy.
25. A statue 1.46 cm tall, stands on the top of a pedestal from a point on the ground, the angle of elevation of the top of the statue is $60^{\circ} \&$ from the same point, the angle of elevation of the top of the pedestal is $45^{\circ}$. Find the height of the pedestal. $\overline{3}=1.73$
26. If the distances of $\mathrm{P} x, y$ from the points $\mathrm{A} 3,6 \& B-3,4$ are equal, prove that $3 x+y=5$.
27. For what value of ' $p$ ', are the points $2,1, p,-1 \&-1,3$ are collinear?
28. From a well-shuffled pack of 52 cards black aces \& black queen are removed. From the remaining cards, a card is drawn at random. Find the probability of drawing a king or a queen.

## Section - 'D'

29. A peacock is sitting on the top of a pillar, which is $9 m$ high. From a point $27 m$ away from the bottom of a pillar a snake is coming to its hole at the base of the pillar. Seeing the snake the peacock pounces on it. If their speeds are equal, at what distance from the hole is the snake caught?

## OR

Two pipes running together can fill a cistern in $2 \frac{8}{11}$ minutes. If one pipe takes one minute more than the other to fill the cistern, find the time in which each pipe would fill the cistern.
30. The sum of the first 20 terms of an A.P. is equal to the sum of first 30 terms. Show that the sum of its first 50 terms is zero.
31. Prove that the intercept of the tangents between two parallel tangents to a circle subtends a right angle at centre.
32. A cylindrical container filled with ice-cream whose diameter is 12 cm \& height is 15 cm . The whole ice-cream is distributed to 10 children in equal cones having hemispherical tops. If the height of the conical portion is twice the diameter of its base, find the diameter of the ice-cream cone.

## OR

A cylindrical measuring jar of internal diameter 8 cm is partially filled with water. One ball of diameter 2 cm \& one cone of radius 2 cm \& height 3 cm are dropped in it. Bothe are submerged in water completely. What will be the change in level of water in jar?
33. A car is travelling on a straight road leading to a tower. From a point at a distance of 500 m from the tower, the angle of elevation of the top of the tower as seen by the driver is $30^{\circ}$. After driving towards the tower fore 10 seconds, the angle of elevation of the top of the tower as seen by the driver is found to be $60^{\circ}$. Find the speed of the car.
34. If the radii of the circular ends of conical buckets which is 45 cm high are $28 \mathrm{~cm} \& 7 \mathrm{~cm}$, find the capacity of the bucket. use $\pi=\frac{22}{7}$

## M. C.Q. Answers:

1. b
2. $b$
3. b
4. $b$
5. b
6. b
7. b
8. c
9. a
10. c
